

LC2 Calculation Policy

Progression in Calculations

Introduction

This policy was created in response to a need across Learning Community 2 schools and after discussion between Headteachers; to have a standard calculation policy that met the National Curriculum guidelines and provided a consistent approach to calculation that could be used within year groups across LC2 schools and as a progression through the phases.

The policy has been developed with a concrete, pictorial and abstract (CPA) approach in order to scaffold and develop pupils' understanding. The CPA approach is relevant across all ages in order to secure understanding and gain conceptual and procedural fluency.

If children are not at age related expectations for their year the policy will be helpful in tracking back to previous learning. This will enable pupils to develop understanding of calculation methods rather than to have to memorise procedures.

We have given an indication of pitch for the stages in our calculation policy.

A note about carrying digits – the examples in this document reflect the variety of carrying methods used across schools.

NB: This is version 2 of the LC2 Calculation Policy and incorporates changes made during the Maths Subject Leader Session on Thursday 19th October 2017.



LC2 Calculation Policy

<u>CONTENTS</u>	
<u>Page</u>	<u>Section</u>
1	LC2 Overview of Approaches by Year Group
2	Addition
10	Subtraction
16	Multiplication
22	Division
27	Appendix A – Progression in Difficulty in Calculations



		EYFS	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Addition	itions. Draw objects.	Combining sets (count all then count on). Partitioning sets and some part part whole. To use a number line practically to add. Use numbers to represent objects, to begin to record.	Combining two parts to make a whole. Part whole model. Starting at the bigger number and counting on. Regrouping to make 10.	Adding three single digits. Partitioning. Column method – no regrouping. Some exchange.	Column method with regrouping (up to 3 digits).	Column method with regrouping. (up to 4 digits).	Column method with regrouping (with more than 4 digits). Column method - decimals - with the same amount of decimal places.	Column method with regrouping. Column method - decimals - with different amounts of decimal places.
ugusta ang	Use concrete & physical representations.	Partitioning. Physically take away objects. To use a number line practically to subtract. Use numbers to represent objects, to begin to record.	Taking away ones. Counting back. Find the difference. Part whole model. Make 10.	Counting back; counting on. Find the difference, part whole model, make 10. Column method - no regrouping. Some exchange.	Column method with regrouping (up to 3 digits).	Column method with regrouping (up to 4 digits).	Column method with regrouping (with more than 4 digits). Column method - decimals - with the same amount of decimal places	Column method with regrouping. Column method - decimals - with different amounts of decimal places.
Muthakeauch	songs. Practical. Mark making.	Doubling. Grouping - making equal groups.	Doubling. Equal groups. Counting in multiples. Arrays (with support).	Doubling /halving. Counting in multiples. Repeated addition arrays - showing commutative multiplication. Include x symbol.	Counting in multiples. Repeated addition Arrays - showing commutative multiplication. Grid method with apparatus.	Grid method (as a step towards long multiplication). Column multiplication. (2 and 3 digit multiplied by 1 digit).	Column multiplication (up to 4 digit numbers multiplied by 1 or 2 digits). Decimals.	Column multiplication (multi digit up to 4 digits by a 2 digit number). Decimals.
Division	Rhymes and s	Doubling/halving. Sharing. Grouping - making equal groups.	Sharing objects. Division as grouping into equal sized groups .	Doubling/halving. Division as grouping and sharing. Division within arrays. Bar model.	Division within arrays. Division with a remainder. Short division (2 digits by 1 digit - concrete and pictorial).	Division within arrays. Division with a remainder / as a fraction. Short division with regrouping (up to 3 digits by 1 digit- concrete and pictorial).	Short division. (up to 4 digits by a 1 digit number - interpret remainders appropriately for the context).	Short division. Long division (up to 4 digits by a 2 digit number - interpret remainders as whole numbers, fractions or round).



Year	Strategy/Approach	Concrete	Pictorial	Abstract
EYFS	Subitising	Children need to recognise a small group of objects/dots/fingers as the total without counting them	Use a range of resources e.g. stones before moving to recording	Pupils recognise amounts without counting.
EYFS Y1	Combining two parts to make a whole: part - whole model	Image: constraint of the second sec	Image: space	Consideration is needed when to introduce symbols. 4 + 3 = 7 10 = 6 + 4 2 + 2 = 3 + 1 Use the part-part whole diagram as shown above to move into the abstract. Looking for patterns in calculations

Year	Strategy/Approach	Concrete	Pictorial	Abstract
		 Underlying skills: Number recognition 0 -10 and the Know that numbers identify how r Recognise numbers and represent Count objects accurately using one each object Know how to write each number Being able to count on from numb 	Vocabulary: add, more, and make, sum, altogether count on group how many? one more, two more, ten more, Same as	
EYFS Y1	Starting at the bigger number and counting on	Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer.	7+4 In jumps of one. 1 + 1 + 1 + 1 + 1 + 1 + 1 + 1 + 1 + 1 +	5 + 12 = 17 Place the larger number in your head and count on the smaller number to find your answer. 'Counting' could be automatic from fluency rather than in ones

Year	Strategy/Approach	Concrete	Pictorial	Abstract
Y1	Regrouping to make 10	6 + 5 = 11	3 + 9 = Use pictures or a number line. Regroup or partition the smaller number to make 10	9 + 5 = 14 If I am at nine, how many more do I need to make 10? How many more do I need to add on now?
		Start with the bigger number and use the smaller number to make 10	9 + 5 = 14 $1 4 + 1 + 4$ $0 + 2 + 3 + 5 + 6 + 7 + 8 (9) (10) + 11 + 12 + 13 (14) + 15 + 16 + 17 + 18 + 19 + 20$	
Y2	Adding three single digits	4 + 7 + 6 = 17 Put 4 and 6 together to make 10. Add on 7.		4 + 7 + 6 = 10 + 7 $= 17$ Combine the two numbers that make 10 and then add on the remainder.
		Following on from making 10, make 10 with 2 of the digits (if possible) then add on the third digit.	Add together three groups of objects. Draw a picture to recombine the groups to make 10.	Emphasising the commutative nature/law 4 + 7 + 6 = 17 7 + 4 + 6 = 17 6 + 7 + 4 = 17



Year	Strategy/Approach	Concrete	Pictorial	Abstract
Y2	Partitioning	Using Dienes Blocks and Base 10	This stage will be used by some children.	64 + 32 = 96 $4 + 2 = 6$ $60 + 30 = 90$ <u>96</u> OR $60 + 30 = 90$ $4 + 2 = 6$ <u>96</u>
Υ2	Start of the vertical (column) method No exchange required WHEN CALCULATIONS ARE REPRESENTED VERTICALLY WE START WITH THE LEAST SIGNIFICANT DIGITS FIRST.	Tens Units Image: Constrained state stat	At this stage pupils can still link this method with partitioning and work with values of ones and tens. Example: 30 + 20 = 50 moving to include the language of 3t + 2t = 5t	24 + 62 = 88 No bridging

Year	Strategy/Approach	Concrete	Pictorial	Abstract	
Y2	Year 2: TO + TO with exchange (no exchange for expected at Y2 but with exchange for greater depth)	Use a range of apparatus – numicon, straws, beads etc.	Some pupils will need to make drawings to represent the concrete. App called Number Pieces	Start by partitioning the numbers before moving on to clearly show the exchange below the addition. 20 + 5 $40 + 8$ $60 + 13 = 73$	
Y3	Column method- regrouping / exchange Year 3: HTO + HTO (no bridging) HTO + HTO (bridging)	Base 10 still needed at concrete stage, then PV counters if appropriate, then abstract. Begin with ones (always).	 Children can draw a pictoral representation of the columns and place value counters to further support their learning and understanding. The language here needs to refer to the place value column For the example on the left the commentary includes 6 ones and 7 ones equals thirteen ones Four tens add two tens plus the extra one 	Expanded method - to be shown as an option to bridge understanding between the pictorial and the abstractContracted method 536 536 $+$ 85 11 $(5+6)$ 110 $(80 + 30)$ 500 (500) 621 11	

Year	Strategy/Approach	Concrete			Pictorial	Abstract	
Y4	Year 4: ThHTO + ThHTO (no carrying) ThHTO + ThHTO (carrying) Year 4 – need 4 digits + 4 digits (decimals too). Base 10 still needed at concrete stage, then PV counters, then abstract. Begin with ones (always).	Add up th for one 10 7 •	e units a		hange 10 ones	The language here needs to refer to the place value column For the example on the left the commentary includes 4 ones and 7 ones equals eleven ones Three tens add one ten plus the extra ten Six hundreds and five hundreds equal 11 hundreds etc	H T OH T O $5 3 6$ 85 $6 2 1$ $5 36$ 85 $6 21$ 1235 1235 7498 1235 7498 11235 7498 11235 7498 11235 7498 11235 7498 11235 7498 11235 7498 11235 7498 11235 7498 11235 7498 11235 7498 11235 7498 11235 7498 11235 7498 11235 8733 1235 7498 11235 8733 1235 7498 11235 8733 1235 </td



Year	Strategy/Approach	Concrete	Pictorial	Abstract
Year Y5	Strategy/Approach Add decimals to 1 and 2 decimal places	Concrete Demonstrate how to exchange across the columns so pupils understand the consistency in relationships in place value including decimals. As children move on to decimals, money and decimal place value counters can be used to support learning. Use money as a way in.	Pictorial Base 10 for decimals Use of place value counters can support pictorial representation of this.	Abstract 72.8 +54.6 127.4 1 1 $\frac{\pounds 2 \ 3 \ . \ 5 \ 9}{\pounds \ 7 \ . \ 5 \ 5}$ $\frac{\pounds 3 \ 1 \ . \ 1 \ 4}{1 \ 1}$ 26.3 $+ \frac{4.9}{41.2}$ $\frac{41.2}{x \ x}$ +1.4
				$\begin{array}{c} 2 & 3 & . & 3 & 6 & 1 \\ & 4 & 1 & . & 2 \end{array}$ $\begin{array}{c} 2 & 3 & . & 3 & 6 & 1 \\ & 9 & . & 0 & 8 & 0 \\ 5 & 9 & . & 7 & 7 & 0 \\ + & 1 & . & 3 & 0 & 0 \\ \hline 9 & 3 & . & 5 & 1 & 1 \\ \hline 2 & 1 & 2 \end{array}$

1C2

Addition

Year	Strategy/Approach	Con		Pictorial					Abstract	
76					nelp pupils t gs when wri		ne place valu culations.	ie column	and the second second	32 52 84 742 582
	Mi	in one	Tth Thousands	H Hunderds	46 · 2 12 · 1 T Tens	0 Ones	t Tenths	h Hundredths	ways.	
		100 000	10 000 1000	169			0,1	0.01	0.001	
					0	00				

Year	Strategy/Approach	Concrete	Pictorial	Abstract
EYFS	Taking away ones	In a practical context, use physical objects, counters, cubes etc to show how objects can be taken away.	Cross out drawn objects to show what has been taken away.	18 -3= 15
		4 - 2 = 2		8 – 2 = 6 (Consideration is needed as to when to use symbols).
EYFS Y1	Counting back	Make the larger number in your subtraction. Move the beads along your bead string as you count backwards in ones. 13 - 4 = 9 Use counters and move them away from the group as you take them away counting backwards as you go.	Count back on a number line or number track. 9 10 11 12 13 14 15 Start at the bigger number and count back – become more efficient using number facts rather than counting in ones. -10	Put 13 in your head, count back 4. What number are you at? Use your fingers to help initially; then knowledge and fluency in number facts. <u>Y2</u> 57 - 23 57 - 23 57 - 20 - 3 37 - 3 34



Year	Strategy/Approach	Concrete	Pictorial	Abstract
Y2	Partition numbers to use 10	Calculations below 30 Dienes blocks Base 10	13 - 7 = 6 3 4 5 + 2 + 3 + 5 + 5 + 5 + 5 + 5 + 10 + 12 + 3 + 4 + 5 + 16 + 7 + 18 + 19 + 20 Start at 13. Take away 3 to reach 10. Then take away the remaining 4 so you have taken away 7 altogether. You have reached your answer.	16 – 8= How many do we take off to reach 10? How many do we have left to take off?
EYFS Y1 Y2	Part Part Whole Model	Link to addition - use the part part whole model to help explain the inverse between addition and subtraction. If 10 is the whole and 6 is one of the parts. What is the other part? 10 - 6 =	Use a pictorial representation of objects to show the part part whole model. $() \qquad () \qquad$	5 10 Move to using numbers within the part whole model. 10-5=5



Year	Strategy/Approach	Concrete	Pictorial	Abstract
Υ2	Find the difference	Compare amounts and objects to find the difference. Image: Compare amounts and objects to find the difference Image: Compare amounts and objects to find the difference Image: Compare amounts and objects to find the difference Image: Compare amounts and objects to find the difference Image: Compare amounts amounts and objects to find the difference Image: Compare amounts amount amounts	+6for the find the difference012012012011 <trr>111<</trr>	Hannah has 23 sandwiches, Helen has 15 sandwiches. Find the difference between the numbers of sandwiches.
Y2 Y3	Column method: No need to regroup or exchange	Start with the ones, or smallest value. Don't write T/O above tens/ones when using the value of the whole number for example '40'. $ \begin{array}{c c} & 40 & 7 \\ \hline & 40 & 7 \\ \hline & 20 & 3 \\ \hline & 20 & 4 \\ \hline & 20 & 4 \\ \hline \end{array} $	Pictorial representation of the concrete.	40 7 - 20 3 20 4



Year	Strategy/Approach	Concrete	Pictorial	Abstract
Y2 (greater depth) Y3 Y4	Column method with regrouping or exchange <i>Initially with two</i> <i>digit numbers</i> When presenting calculations vertically pupils are taught to start with the least significant digit.	-40 3 30 13 -20 7 10 6	Say the values of the numbers: Forty and five subtract twenty and seven. Five subtract seven – I don't have enough. So I take ten from forty and add it to the five. I now have thirty and fifteen. I now can take seven from fifteen which is eight. Then twenty from thirty which is ten.	³⁰ 15 40 5 - 20 7 10 8
			Connect the place value column: 5 ones subtract 7 ones – I don't have enough so I will exchange a ten from the four tens leaving three tens and 15 ones. Now I have 3 tens subtract 2 tens.	$ \begin{array}{r} 3 & 1 \\ 4 & 5 \\ - \frac{2 7}{1 8} \end{array} $



Column method with Y3 regrouping or exchange

Larger numbers

More than one exchange required

Extends to decimals

Year 3: HTO - HTO (no exchange)

HTO - HTO (exchange)

Y4

Year 4: ThHTO - ThHTO (one digit exchanging)

ThHTO - ThHTO (more than one digit exchanging)

Subtract decimals to 1 and then 2 decimal places.

Use Base 10 to start with before moving on to place value counters. Start with one exchange before moving onto subtractions with 2 exchanges.

1 Make the larger number with the place value counters.



<u>2</u> Start with the ones, can I take away 8 from 4 easily? I need to exchange one of my tens for ten ones.



<u>3</u> Now I can subtract my ones.



4

Now look at the tens, can I take away 8 tens easily? I need to exchange one hundred for ten tens.



5

Now I can take away eight tens and complete my subtraction.



Show children how the concrete method links to the written method alongside your working. Cross out the numbers when exchanging and show where we write our new amount.



Children can start their formal written method by partitioning the number into clear place value columns.

Y4 728-582=146 12 8 8 2 5 4 6

Moving forward the children use a more compact method.

This will lead to an understanding of subtracting any number including decimals.



6

<u>Subtraction</u>

Year	Strategy/Approach	Concrete	Pictorial	Abstract
Y5	Further stages in the method Year 5: Calculations with more than 4 digits including decimals with same number of digits Year 6: Calculations including decimals with different decimal values Ensure vocabulary and language is consistent across year groups – for example, exchange, regroup, steal.		$\begin{array}{r} e \cdot g \\ 3 & 12 \\ 4 \cdot 2 \cdot 12 \\ 1 & 7 \cdot 6 \\ \hline 2 & 5 \cdot 6 \\ \hline \\ (4 \cdot 3 \cdot 2 - 17 \cdot 6) \\ \hline \\ 2 \cdot g \\ \hline \\ 4 \cdot 10 \cdot 12 \\ 1 & 3 \cdot 6 \\ \hline \\ \hline \\ 1 & 3 \cdot 6 \\ \hline \\ \hline \\ 2 & 6 \cdot 6 \\ \hline \\ (4 \cdot 02 - 13 \cdot 6) \end{array}$	$\begin{array}{c} \underline{e_{9}} & 47.12 - 13.7 \\ 47.112 \\ 13.70 - \\ \hline 33.42 \\ \underline{e_{9}} \\ 316 \\ 14.7 \\ 29.6 \\ \hline 1 \\ 117.44 \end{array}$
		Some pupils may find it useful to continue with the place value column headings.	$43.7 - 3\frac{3}{4} \longrightarrow 43.70$ $- 3.25$ $4 - 3.75 \longrightarrow 4.00$ $- 3.75$	



Year	Strategy/Approach	Concrete	Pictorial	Abstract
EYFS Y1	Doubling	Use practical activities to show how to double a number.	Draw pictures to show how to double a number.	
Y2			Double 4 is 8	
		double 4 is 8		²⁰ 12 32
		4 × 2 = 8		Partition a number and then double each part before recombining it back together.
Y1	Counting in multiples		man way on any	Count in multiples of a number aloud.
		and the second second		Write sequences with multiples of numbers.
				2, 4, 6, 8, 10
		Count in multiples supported by	Use a number line or pictures to continue support in counting in multiples.	5, 10, 15, 20, 25 , 30
		Count in multiples supported by concrete objects in equal groups. Ensure that pupils do not count in ones.		



Year	Strategy/Approach	Concrete	Pictorial	Abstract
Υ2	Repeated addition of equal groups	5 + 5 + 5 $i = 5$	There are 3 plates. Each plate has 2 star biscuits on. How many biscuits are there? 2 add 2 add 2 equals 6 5 + 5 + 5 = 15	Write addition sentences to describe objects and pictures. $\sum_{2+2+2+2+2=10}^{2}$
Υ2	Arrays – showing commutative multiplication	Create arrays using counters/ cubes to show multiplication sentences.	Use arrays in different rotations to find commutative multiplication sentences. 4 × 2=8 2 × 4=8 2 × 4=8 2 × 4=8 4 × 2=8 2 × 4=8 4 × 2=8 2 × 4=8 4 × 2=8 2 × 4=8 4 × 2=8 1 × 4=8 2 × 4=8 4 × 2=8 2 × 4=8 5 × 4	Use an array to write multiplication sentences and reinforce repeated addition. 5+5+5=15 3+3+3+3+3=15 $5 \times 3 = 15$ $3 \times 5 = 15$



Year	Strategy/Approach	Concrete	Pictorial	Abstract
Y3	Towards column multiplication 2 digits x 1 digit	Children can continue to be supported by place value resources at this stage of multiplication. 4 $\begin{pmatrix} 10 & 3 \\ 40 & 12 \\ 12 \\ 12 \\ 12 \\ 12 \\ 12 \\ 12 \\ 12$	$4 \begin{array}{c} 10 & 3 \\ 40 & 12 \\ \hline 40 + 12 = 52 \end{array}$	$ \begin{array}{r} 13 \\ x & 4 \\ 12 \\ 40 \\ 52 \end{array} $ $ 13 \times 4 = 52 $
Y4	Towards column multiplication 2 and 3 digits multiplied by 1 digit		$3 \times 123 = 300 + 60 + 9$ $3 \times 123 = 300 + 60 + 9$ $3 \times 123 = 300 + 60 + 9$ $1 (1 (1))$ $3 \times 100 = 300$ $3 \times 20 = 60$ $3 \times 3 = 9$	123 x <u>3</u> 9 60 + <u>300</u> 369



Year	Strategy/Approach	Concrete	Pictorial	Abstract
Y3 Y4	Towards column multiplication Up to 4 digits by 1 digit	$8 \times 23 \qquad \bigcirc $	$33 \times 4 \text{ (grid method)}$ $4 \begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	Expanded 33 x 4 12 (4 x 3) 120 (4 x 30) 132
Y5	Towards column multiplication	$\begin{array}{c} \text{Grid towards long mu} \\ 24 \times 16 \\ 20 & 4 \\ 10 \\ \hline 200 & 40 \\ 6 \\ \hline 120 & 24 \\ \hline \pm 144 \\ \underline{384} \end{array}$	Iltiplication 2 4 24×16 becomes x 1 6 2 4 2 4 $6x4$ $\frac{\times}{2}$ 4 2 4 $6x4$ $\frac{\times}{2}$ 4 2 0 $6x20$ $\frac{1}{4}$ 4 4 0 $10x4$ $\frac{3}{3}$ 8 4 2 0 0 Answer: 384 3 8 4 4 4	$ \begin{array}{r} +2 \\ 2 & 4 \\ x & 1 & 6 \\ \hline 1 & 4 & 4 \\ 2 & 4 & 0 \\ \hline 3 & 8 & 4 \end{array} $



Strategy/Approach	Concrete	Pictorial	Abstract
Column multiplication	It is important at this stage that they always multiply the ones first and note down their answer followed by the tens which they note below.	Bar modelling and number lines can support learners when solving problems with multiplication alongside the formal written methods.	Start with long multiplication, reminding the children about lining up their numbers clearly in columns.
	$4 \times 116 =$	Find the form th	If it helps, children can write out what they are solving next to their answer. $\begin{array}{c}32\\x \ 24\\8\\(4 \times 2)\\120\\(4 \times 30)\\40\\(20 \times 2)\\600\\(20 \times 30)\\768\end{array}$ $\begin{array}{c}7\\4\\\\ \hline \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\$
	Column	Column multiplication It is important at this stage that they always multiply the ones first and note down their answer followed by the tens which they note below. $4 \times 116 =$ $100 \ 10 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1$	Column multiplication It is important at this stage that they always multiply the ones first and note down their answer followed by the tens which they note below. $4 \times 116^{\pm}$ $(10) (1) (1) (1) (1) (1) (1) (1) (1) (1) (1$



Year	Strategy/Approach	Concrete	Pictorial	Abstract
				$ \begin{array}{r} +1 \\ +1 \\ +1 \\ 7 \\ 1 \\ 4 \\ 7 \\ x \\ 2 \\ 4 \\ +1 \\ 5 \\ 8 \\ 2 \\ 9 \\ 4 \\ 0 \\ 3 \\ 5 \\ 2 \\ 8 \\ 2 \\ 8 \\ 2 \\ 8 \\ 2 \\ 8 \\ 2 \\ 8 \\ 3 \\ 5 \\ 2 \\ 8 \\ 3 \\ 5 \\ 2 \\ 8 \\ 3 \\ 5 \\ 2 \\ 8 \\ 3 \\ 5 \\ 2 \\ 8 \\ 5 \\ 8 \\ 3 \\ 5 \\ 2 \\ 8 \\ 5 \\ 8 \\ 8 \\ 5 \\ 8 \\ 5 \\ 8 \\ 5 \\ 8 \\ 8 \\ 5 \\ 8 \\ 8 \\ 5 \\ 8 \\ 8 \\ 5 \\ 8 \\ 8 \\ 5 \\ 8 \\ 8 \\ 5 \\ 8 \\ 8 \\ 5 \\ 8 \\ 8 \\ 5 \\ 8 \\ 8 \\ 5 \\ 8 \\ 8 \\ 8 \\ 5 \\ 8 \\ 8 \\ 8 \\ 8 \\ 8 \\ 8 \\ 8 \\ 8 \\ 8 \\ 8$
Y6	Column multiplication Pupils using a column must always start from the right			1342 x 18 13420 13420 10736 24156

Year	Strategy/Approach	Concrete	Pictorial	Abstract
EYFS Y1	Sharing objects into equal groups	10, I have 10	Children use pictures or shapes to share quantities.	Share 9 buns between three people. 9 ÷ 3 = 3
		cubes, can you share them equally in 2 groups?	\$ \$ \$ 8 ÷ 2 = 4	Introduce symbols when appropriate
Y1	Division as grouping	Divide quantities into equal groups.	Use a number line to show jumps in groups. The	
Y2	Concrete in Y1	Use cubes, counters, objects or place value counters to aid understanding.	number of jumps equals the number of groups.	28 ÷ 7 = 4
	Moving to abstract in Y2		$\begin{array}{cccccccccccccccccccccccccccccccccccc$	Divide 28 into 7 groups. How many are in each group?
		How many groups of 2 are in 10?	Think of the bar as a whole. Split it into the number	7 44 24 20
		Share 10 into groups of 2 is 5 groups 10 ÷ 2 = 5	of groups you are dividing by and work out how many would be within each group.	7 14 21 28 28÷7=4
		••••• •••••• ••••• ••••• <t< td=""><td>20</td><td>2 4 6 8 10</td></t<>	20	2 4 6 8 10
		How many groups of 5 are in 35?	20 ÷ 5 = ?	10 ÷ 2 = 5
		An early step <u>could</u> include this language leading to 'division'!	5 x ? = 20	Consider in Y1 Expected in Y2



Year	Strategy/Approach	Concrete	Pictorial	Abstract
Y2	Division within arrays			Find the inverse of multiplication and division sentences by creating four linking number sentences.
		Link division to multiplication by creating an array and thinking about the number sentences that can be	$\bigcirc \bigcirc $	7 x 4 = 28 4 x 7 = 28
		created.	Use and draw an array and use lines to split the	28 ÷ 7 = 4
		Eg: 15÷3=5 5 x 3=15	array into groups to make multiplication and division sentences.	28 ÷ 4 = 7
		15 ÷ 5 = 3 3 x 5 = 15		
Y2 (greater depth)	Division with a remainder	14 ÷ 3 = Divide objects into equal groups and see how much is left over	Jump forward in equal jumps on a number line then see how many more you need to jump to find a remainder.	Complete written divisions and show the remainder using r.
Y3			Initially draw dots and group them to divide an amount and clearly show a remainder.	$\begin{array}{l} 29 \div 8 = 3 \text{ REMAINDER 5} \\ \uparrow \uparrow \uparrow & \uparrow \\ \text{dividend divisor quotient} & \text{remainder} \end{array}$
			() () () () () () () () () ()	
			Develop to more efficient recording as below.	
			$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	

Year	Strategy/Approach	Concrete	Pictorial	Abstract
Y3	Start of chunking which develops to		<u>13 divided by 4</u> 4 13	It is important to develop efficiency.
	become more efficient		$\bigcirc \bigcirc \bigcirc \bigcirc -4 \\ \hline 9 \\ \hline 9 \\ \hline $	$21 \div 4 = 5 r 1 \qquad \textcircled{1}{21} 5 r 1 \\ 4 \boxed{21} \\ - 4 (1 \times 4)$
	Consider introducing the short division		$\bigcirc \bigcirc \bigcirc \bigcirc -4 \\ 5 \\ \hline$	$ 17 4 (1 \times 4) 13 4 (1 \times 4) 9 9 $
	method		$\bigcirc \bigcirc \bigcirc \bigcirc -4$	$ \begin{array}{r} 9 \\ - 4 \\ 5 \\ -4 \\ 1 \end{array} $
			Can I make a group of 4?" "Can I make another group of 4?"	Becoming more efficient and progressing to: 5 r 1 <u>4121</u> <u>- 20</u> (5 x 4) <u>1</u>
			$\begin{array}{c c} 4 & 1 & 3 \\ & -1 & 2 \\ \hline & 1 \end{array}$	
			24 divided by 5	12 6 72 -60 (10 x)
Y4	Division with a remainder/as a fraction	Short division becoming more efficient i.e. subracting in larger chunks.	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	12 -12 (2 x) 0

Year Strategy/Approach	Concrete	Pictorial	Abstract
 /3 Division with regrouping / /4 exchange is introduced in Y3/Y4 Practical n the next consider n 	dienes nodelling of the example in olumn. nodelling process with umbers to develop		98 ÷ 7 becomes $1 4$ 7 9^{2} 8 Answer: 14 432 ÷ 5 becomes $432 ÷ 5 becomes$ $\frac{8 6}{5} r^{2}$ 5 $4 3^{3} 2$ Answer: 86 remainder 2 496 ÷ 11 becomes $\frac{4 5 r 1}{1 4 9 5 6}$ Answer: 45 $\frac{1}{11}$

Year	Strategy/Approach	Concrete	Pictorial	Abstract
	Short division with larger numbers		Some children would benefit from the 'I Know' box.	1 2 4 r2 ^{3 5} 1 4 1 7 3 8
Y5 Y6	Dividing 4 digits by 2 digits using long division		1738 ÷ 14 $ \begin{array}{ccccccccccccccccccccccccccccccccccc$	'I Know' boxes are used to find efficient answers e.g. first subtraction when dividing hundreds are likely to be hundreds/tens.



ADDITION	SUBTRACTION
 No exchange Extra digit in the answer Exchanging ones to tens Exchanging tens to hundreds Exchanging ones to tens and tens to hundreds More than two numbers in calculation As 6 but with different number of digits Decimals up to 2 decimal places (same number of decimal places) Add two or more decimals with a range of decimal places 	 No exchange Fewer digits in the answer Exchanging tens for ones Exchanging hundreds for tens Exchanging hundreds to tens and tens to ones As 5 but with different number of digits Decimals up to 2 decimal places (same number of decimal places) Subtract two or more decimals with a range of decimal places
SHORT MULTIPLICATION	SHORT DIVISION
 TO x O no exchange TO x O extra digit in the answer TO x O with exchange of ones into tens HTO x O no exchange HTO x O with exchange of ones into tens HTO x O with exchange of tens into hundreds HTO x O with exchange of ones into tens and tens into hundreds As 4-7 but with greater number digits x O O.t x O no exchange O.t with exchange of tenths to ones As 9 - 10 but with greater number of digits which may include a range of decimal places x O 	 TO ÷ O no exchange no remainder TO ÷ O no exchange with remainder TO ÷ O with exchange no remainder TO ÷ O with exchange, with remainder Zero in the quotient e.g. 816 ÷ 4 = 204 As 1-5 HTO ÷ O As 1-5 greater number of digits ÷ O As 1-5 with a decimal dividend e.g. 7.5 ÷ 5 or 0.12 ÷ 3 Where the divisor is a two-digit number Remainders Whole number remainder Remainder expressed as a fraction of the divisor Remainder expressed as a decimal